



# Comparison of interpolation-based sampling frequency offset compensation schemes for practical OFDM-VLC systems

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**Abstract:** Sampling frequency offset (SFO) is an important issue in the orthogonal frequency-division multiplexing (OFDM)-based visible light communication (VLC) systems with low-cost analog-to-digital or digital-to-analog converters (ADCs/DACs). A digital interpolation or resampling filter can be used to effectively compensate the SFO. In such case, oversampling at the receiver ADC is required to mitigate the aliasing effect due to imperfect DACs and nonlinearity of visible light sources that cause extra frequency components inside/outside the OFDM signal spectrum. The oversampling factor (rate) is mainly determined by the order of the digital interpolation filter and nonlinear VLC links. The design of the OFDM-VLC receiver incorporating the digital interpolation filter is vital as it affects not only the transmission performance but also the complexity of digital signal processing (DSP). To evaluate the feasibility of the digital interpolation-based SFO compensation schemes for cost-sensitive VLC applications, in this paper, a real-time OFDM-VLC receiver incorporating the 2<sup>nd</sup>/3<sup>rd</sup>/4<sup>th</sup> order interpolation filters is experimentally demonstrated. An OFDM frame structure is designed for the synchronization including SFO estimation and compensation, in which the precision and latency of DSP are considered. On the basis of the real-time OFDM-VLC receiver, the comparison in the VLC transmission performance and DSP complexity between different interpolation-based SFO compensation schemes is discussed.

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## 1. Introduction

To satisfy the ever-increasing data traffic in the current communication networks and the demand for high-speed transmission, much attention has been paid to visible light communication (VLC) in recent years. In particular, VLC has become a favorable complementary technology to millimeter-wave communication in short-range communication scenarios for future wireless networks [1–8]. For the indoor applications, as an example, it not only relieves spectral congestion in the current industrial, scientific, medical (ISM) radio band, but also provides multiple gigabit-per-second data transmission with spectral-efficient modulation techniques [2,5]. One of these techniques is orthogonal frequency-division multiplexing (OFDM) applied to improve spectral efficiency of the white light emitting diodes (LEDs)-based VLC systems [5,7]. In practice, short-range OFDM-VLC systems are cost-sensitive, in which sampling frequency offset (SFO) occurs between low-cost analog-to-digital or digital-to-analog converters (ADCs/DACs). SFO is an important issue as it causes accumulated phase rotation and severe interference between OFDM subcarriers (inter-carrier interference, ICI) [9]. Moreover, the LED nonlinearity causes extra spectral components within and beyond the OFDM signal spectrum, which affects the synchronization performance [10,11]. Although a number of methods were suggested to compensate the nonlinear distortion [12,13], most of these methods are able to

compensate the second order distortion in a practical VLC system with low complexity. Residual distortion still exists after the nonlinear compensation for a VLC link with high order nonlinear distortion. Therefore, precise synchronization is required in a cost-sensitive OFDM-VLC system.

With the rapid development of complementary metal oxide semiconductor (CMOS)-based digital electronics, high-speed hardware for digital signal processing (DSP) including DACs/ADCs has been widely used for optical communications. DSP becomes practical and attractive as it offers many advantages including flexibility and low complexity compared to traditional analog signal processing. As a result, DSP-based synchronization is a preferable option. To compensate the SFO in the digital domain, a digital interpolation or resampling filter can be used to reconstruct or resample the received signal for OFDM decoding. Prior to the DSP, the ADC usually operates at a sampling frequency (oversampling) higher than the Nyquist frequency in order to mitigate the aliasing effect due to imperfect DACs and nonlinearity of visible light sources. The oversampling factor (rate) is mainly determined by the interpolation schemes (order of the digital interpolation filter) and nonlinear VLC links. A high oversampling rate may improve the transmission performance, but increase the DSP complexity. To achieve a balance between the performance and complexity, low-level modulation formats requiring a relatively low signal-to-noise ratio (SNR) can relax the oversampling requirement as the transmission performance is tolerant of the SFO-induced ICI at a certain level. However, this results in decrease in system capacity. Therefore, it is vital to design a proper VLC receiver incorporating the digital interpolation filter, which affects not only the VLC transmission performance but also the DSP complexity.

In the literature, there is rare study about real-time investigation of OFDM synchronization for VLC applications. Most investigations in a real-time system are relevant to digital predistortion waveform shaping [14,15], equalization [16] and reduction of peak-to-average-power ratio (PAPR) [17]. In the publication [18], a training symbols-based SFO estimation was applied to compensate the phase error in a real-time laser-based VLC system, whilst the SFO-induced ICI still exists. To minimize the SFO, costly DACs/ADCs were used to achieve an SFO of approximately 12 ppm so that the SFO effect was negligible [19]. In addition, a voltage-controlled oscillator can supply an accurate frequency for the ADC [20]. However, such a method requiring extra electrical components increases the system cost and complexity.

We proposed a fourth order polynomial interpolator using the Farrow structure to digitally compensate SFO between the transmitter and receiver oscillators for VLC systems [10]. The Farrow structure has a typical property of anti-imaging for the sampling rate conversion applications when the sampling rate is increased [21]. Compared with the conventional fractional delay filter-based interpolators that require a large size lookup table for mapping a variable delay, the Farrow structure-based interpolators have advantages of low complexity and good flexibility. This is because the fixed coefficients of filters related to impulse responses are applied in the Farrow structure, whilst the only input variables are the fractional interval and integer number of samples. Experimental results with offline signal processing show that the proposed scheme can be used to effectively compensate a local frequency offset up to  $\pm 1000$  ppm at a minimum oversampling rate of 1.3 in an OFDM-based VLC system [10]. In the offline signal processing, the received signal was captured by a digital oscilloscope, in which signal recovery was carried out with Matlab. It is obvious that the precision and latency of DSP functions were not considered.

To explore the transmission performance with real-time signal processing, we further demonstrated a field-programming-gate-array (FPGA)-based OFDM-VLC receiver incorporating the synchronization function in [22], where discussions about the whole DSP design and complexity were not given. In this paper, significantly extended investigation is made on a detailed evaluation of the digital interpolation-based SFO compensation scheme with real-time DSP at the OFDM-VLC receiver. In addition, an OFDM frame structure is designed for the synchronization including

SFO estimation and compensation. The comparison in the VLC transmission performance and DSP complexity between different SFO compensation schemes employing a 2<sup>nd</sup>/3<sup>rd</sup>/4<sup>th</sup> order interpolation filter is discussed.

## 2. OFDM-based VLC receiver with digital SFO estimation and compensation

### 2.1. Signal reconstruction with the Farrow structure-based interpolator

In a typical OFDM-VLC system with an incoherent light source (LED) as shown in Fig. 1, intensity modulation and direct detection is generally applied for short-range communications. With a DAC operating at a sampling rate of  $f_t$ , the analog OFDM signal driving the LED can be expressed as,

$$z(t) = V_b + u \sum_{k=1}^{N/2-1} Z(k) \cos(2\pi k f_t t / N) \quad t \in [0, N/f_t] \quad (1)$$

where  $V_b$  and  $u$  are bias voltage of the LED and linear gain/attenuation of electrical components, respectively.  $t$  is a time variable.  $Z(k)$  is the information data carried on the  $k$ -th subcarrier in a symbol period.  $N$  is the number of subcarriers in the positive and negative frequency range. Owing to the nonlinear transfer function of the LED for electrical-to-optical conversion, the transmitted signal is distorted seriously after the electrical-to-optical conversion. To better understand the nonlinear effect, a simplified polynomial form is used to model the LED nonlinearity [11,23]. The optical intensity of the transmitted signal can thereby be written as,

$$p(t) = \sum_{j=1}^M b_j z^j(t) + b_0 \quad (2)$$

where  $b_j$  is the coefficient of the  $j$ -th linear/nonlinear term.  $b_0$  is constant and  $M$  is the highest order of the nonlinear distortion ( $M \geq 2$ ). After light propagation over a VLC link, the received optical signal is converted by a photodiode (PD) into the electrical signal,  $x(t)$ , in the following form [24].

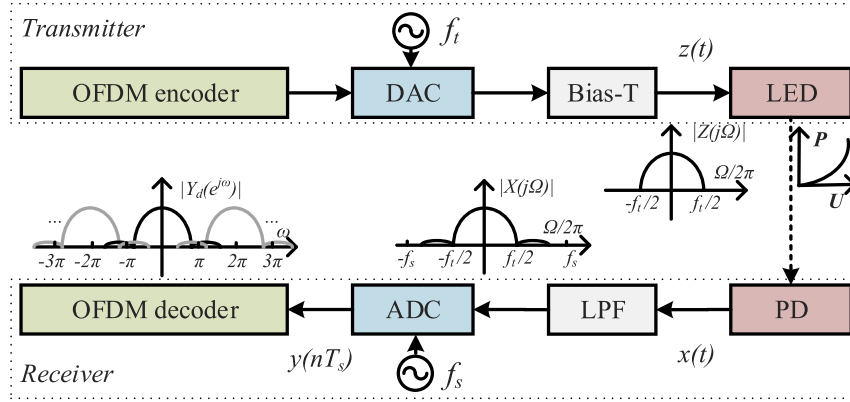
$$x(t) = p(t) \otimes h_v(t) + w(t) \quad (3)$$

$$h_v(t) = \eta e^{-2\pi k_L f_L t} u(t) \otimes e^{-2\pi k_P f_P t} u(t) \otimes h_B(t) \quad (4)$$

where  $h_v$  is linear impulse response of the VLC link including the LED, PD and electrical amplifiers.  $w(t)$  is sum of shot noise and thermal noise at the receiver, which is usually modeled as additive white Gaussian noise (AWGN) [25].  $\eta$  is attenuation coefficient.  $f_L$  ( $f_P$ ) is the 3-dB bandwidth of the LEDs (PDs) that is modelled with a low pass filter (LPF).  $k_L$  and  $k_P$  are the fitted coefficients.  $u(t)$  is the unit step function, and  $h_B(t)$  is the impulse response of a high-pass filter. From Eqs. (2) and (3), new frequency components are induced within and beyond the OFDM spectrum so that the received signal spectrum is broadened widely as shown in Fig. 1.

In addition, because of the instability of the transceiver oscillators, the sampling frequency of the DAC at the transmitter may not be equal to that of the ADC at the receiver,  $f_s = 1/T_s = \lambda f_t (1 + \eta)$ .  $\lambda$  is oversampling rate and  $\eta$  is SFO. Without proper SFO compensation in the nonlinear VLC link, the ICI and the outband frequency components cause performance degradation on the signal recovery in the OFDM decoder. Detailed description of the OFDM-VLC system with the digital SFO compensation can be found in [10]. The principle of digital SFO compensation is briefly introduced, whilst a DSP design and an OFDM frame structure for the OFDM-VLC receiver are discussed in details in this section.

The spectral aliasing effect resulted from the SFO and LED nonlinearity can be mitigated by digitally resampling the received signal with a Farrow-structured interpolator. It is noted that the digital interpolator is applied to compensate the SFO instead of the LED nonlinearity in a nonlinear VLC link. As shown in Fig. 2, the Farrow structure consists of  $Q + 1$  columns of finite

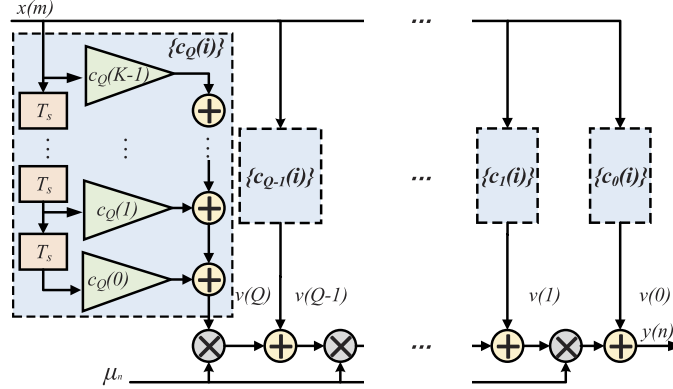


**Fig. 1.** Schematic diagram of a typical OFDM-VLC system with an LED-based intensity modulator.

impulse responses (FIRs) filters with  $K$  taps. In each FIR filter, fixed tap coefficients are applied. The resampled signal at an estimated sampling period ( $T_i$ ) is thereby given below [26]

$$y(nT_i) = \sum_{i=0}^{K-1} x[(m_n - i)T_s] \cdot h_i[(i + \mu_n)T_s] = \sum_{q=0}^Q \mu_n^q v(q) \quad (5)$$

$$v(q) = \sum_{i=0}^{K-1} c_q(i) x[(m_n - i)T_s] \quad (6)$$



**Fig. 2.** A polynomial interpolator with the Farrow structure.

$c_q(i)$  is coefficient of the interpolation filter using the Farrow structure.  $v(q)$  is output of the FIR filter.  $m_n$  and  $\mu_n$  are input variables that determine the position of the reconstructed sample,

$$m_n = \text{int}[nT_i/T_s] = \text{int}[n\lambda(1 + \eta')] \quad (7)$$

$$\mu_n = nT_i/T_s - m_n = n\lambda(1 + \eta') - m_n \quad (8)$$

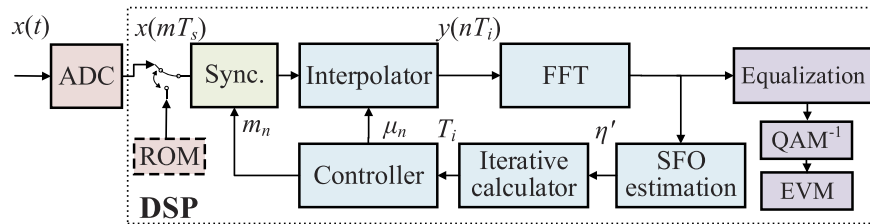
$$T_i = \lambda(1 + \eta')T_s \quad (9)$$

where the operator  $\text{int}[x]$  means the largest integer not exceeding  $x$ .  $\mu_n$  is called the fractional interval specified in the interval  $0 \leq \mu_n < 1$ . It is noted that  $h_i$  is the time-varying impulse response of the interpolation filter, which depends on the fractional interval. As the Farrow structure

requires only the variable  $\mu_n$  for each interpolation, the precision of the interpolation mainly depends on the calculation of the  $\mu_n$ . The accuracy of the  $\mu_n$  is determined by the SFO estimated with pilot subcarriers,  $\eta'$ . Moreover, the adjustment of the  $\mu_n$  in such a structure is easier than the structure of the conventional interpolation filters utilizing lookup tables.

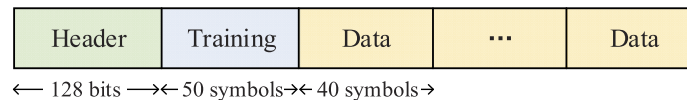
## 2.2. DSP design

To design a practical VLC receiver that mitigates the SFO effect based on the aforementioned principle, a block diagram of the DSP in the OFDM-VLC receiver with the OFDM synchronization is given in Fig. 3. The digitized signal after the ADC is recovered by the DSP functions including synchronization, SFO estimation/compensation, fast Fourier transform (FFT), equalization and quadrature amplitude modulation (QAM) demapping. The synchronization function is applied to detect the start of an OFDM frame/symbol. Error vector magnitude (EVM) is calculated for quantifying the transmission performance. It is noted that as a feedback loop is applied to track the SFO estimated after the FFT, there is a delay of up to two symbol periods (FFT and SFO estimation) in compensating the SFO, which is usually not considered in the simulation or offline signal processing. This usually requires a training sequence added before the information data, which is related to the design of the frame structure to be discussed in the following part.



**Fig. 3.** Block diagram of the DSP in the OFDM-VLC receiver. Sync: synchronization.

In general, the received signal sequence including the training and information data is organized in a frame for the purposes of synchronization and channel estimation. To this end, a frame structure of the OFDM-VLC signal is designed in Fig. 4. At the beginning of each frame, a synchronization header consisting of 128 bits encoded with on-off keying (OOK) is used for the frame synchronization. As the main concern is focused on the synchronization performance, a simple zero-forcing channel estimation is applied to estimate the channel state information (CSI) with a training sequence block containing 50 OFDM symbols. The length of training symbols can be reduced with advanced channel estimation methods in practice. Following the channel estimation, the SFO is estimated with the phase difference of 4 pilot subcarriers between two OFDM symbols delayed by 4 symbols when the size of FFT is 128 [10]. To improve the estimation accuracy, a number of OFDM symbols ( $\leq 40$ ) are used to average the estimated SFO. Therefore, every 40 OFDM symbols including pilot and information subcarriers form a data block for update of the estimated SFO. Because of the relatively stable VLC channel, the number of data blocks is generally large, which is determined by the dynamic feature of the VLC links. Compared with the offline signal processing that updates the estimated SFO in each symbol period, the practical real-time signal processing has a relatively slow update rate.



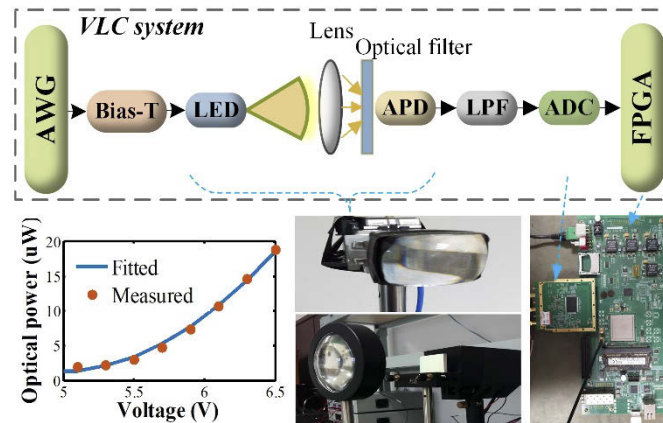
**Fig. 4.** Designed frame structure of the OFDM-VLC signal.



It is noted that to avoid the effect of imperfect ADCs, a Read Only Memory (ROM) storing simulated signals is selectively used to evaluate the DSP design of the OFDM synchronization in the VLC system. After the signal reconstruction with the Farrow-structured interpolators, normal OFDM decoding is applied. The 2<sup>nd</sup>/3<sup>rd</sup>/4<sup>th</sup> order interpolation filters are considered for performance comparison in the next section.

### 3. Comparison in real-time transmission performance and DSP complexity

Following the discussion about the design of the OFDM-VLC receiver including the frame structure and interpolation structure for digital SFO compensation in Section 2, an FPGA-based OFDM-VLC receiver was developed to explore the feasibility of the interpolation-based SFO compensation schemes. An OFDM-VLC system as shown in Fig. 5 was established for the experimental exploration. Since the motivation of this study is to experimentally investigate the real-time performance of the SFO compensation at the OFDM-VLC receiver, an arbitrary waveform generator (AWG) was used as a transmitter for signal generation. More importantly, the application of the AWG allows us to finely adjust the sampling frequency of DAC for a specific SFO. The experimental setup of the VLC system was almost the same as that in [10] except the developed real-time OFDM-VLC receiver. The DSP design for the real-time receiver with the aforementioned synchronization algorithm was transformed to a hardware design with a DSP tool (System Generator from Xilinx). The signal recovery was conducted with the DSP on a FPGA evaluation board (Xilinx Virtex-6). Table 1 lists default values of key parameters unless explicitly mentioned.



**Fig. 5.** Experimental setup of the OFDM-VLC system.

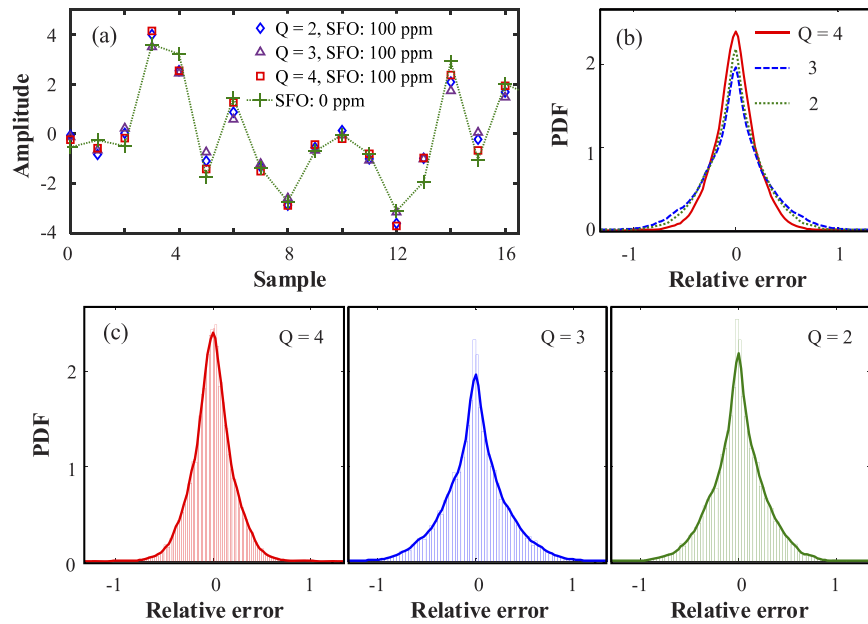
#### 3.1. Verification of the DSP design

Prior to experimental investigation of the real-time transmission performance over the VLC link, experimental evaluation of the synchronization scheme was initially conducted on a single FPGA board as seen in Fig. 6. The data of the simulated OFDM signal with an arbitrary SFO was stored in the ROM as the input of the FPGA receiver. In such case, the noise in the receiver was assumed to be negligible, whilst only the SFO effect was considered. Figure 6(a) shows waveforms constructed with the 2<sup>nd</sup>, 3<sup>rd</sup>, 4<sup>th</sup> order interpolators where SFO = 100 ppm,  $\lambda = 1.3$ . It is clear to see that the waveform reconstructed with the 4<sup>th</sup> order interpolator is closer to the waveform with SFO = 0 ppm compared with the 2<sup>nd</sup> and 3<sup>rd</sup> order interpolators.

To gain a good understanding of the quality of the reconstructed signal in Fig. 6(a), the statistical performance is presented in Figs. 6(b) and 6(c). The probability density functions

Table 1. Key parameters of the OFDM-VLC system

Parameter	Default value
Modulation format	16QAM-OFDM
Size of FFT	128
Cyclic prefix	16
Pilot subcarriers	12 <sup>th</sup> , 23 <sup>rd</sup> , 34 <sup>th</sup> , 45 <sup>th</sup>
Bias voltage (LEDs)	5.75 V
PTP of the drive signal	0.4 V
3-dB bandwidth of LEDs	6 MHz
Coefficients $b_2$ , $b_1$ , $b_0$	$[0.7, -7.2, 18.0] \times 10^{-5}$
Diameter of the lens	10 cm
Cut-off frequency (APD)	40 MHz
Photosensitive area (diameter, APD)	3 mm
Resolution of DACs (AWG)	14 bits
Resolution of ADCs	14 bits
Sampling rate (ADC)	25 or 50 MS/s
Bit rate	25.7 ~ 43.8 Mb/s
Distance	6 m

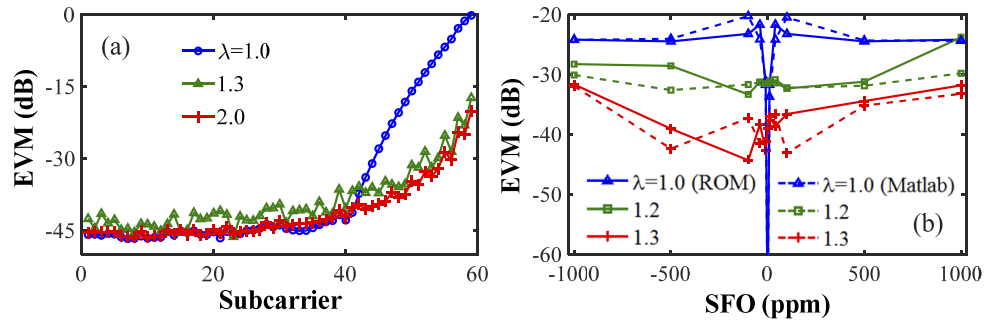


**Fig. 6.** (a) Waveforms constructed with the 2<sup>nd</sup>, 3<sup>rd</sup>, 4<sup>th</sup> order interpolators. (b) Comparison of fitted PDFs, (c) PDF of reconstructed signal errors. SFO = 100 ppm,  $\lambda=1.3$ .

(PDFs) of the relative error of the reconstructed signal were calculated with 14,000 samples when SFO = 100 ppm. The relative error is defined as a ratio of difference between the interpolated signal and the ideal signal to the root mean square of the ideal signal. A Gaussian distribution was used to fit the measured PDF in Fig. 6(c), whilst all fitted PDF curves are plotted for comparison in Fig. 6(b). The variance of 0.042 for the 4<sup>th</sup> order interpolator is smaller than that of the 2<sup>nd</sup>

(0.071) and 3<sup>rd</sup> (0.095) order interpolators. As a result, the fitted PDF curve with the 4<sup>th</sup> order interpolator is narrower than the other interpolators. This indicates the advantage of high order interpolators for reconstruction of the OFDM signal.

Figure 7(a) shows the EVM on each subcarrier using the 4<sup>th</sup> order interpolator at different oversampling rates. Owing to the four pilot subcarriers (12<sup>th</sup>, 23<sup>rd</sup>, 34<sup>th</sup>, 45<sup>th</sup>) allocated in each OFDM symbol for the SFO estimation, only 59 subcarriers are plotted in the figure. For  $\lambda=1.0$ , the EVM on the high frequency subcarriers (40~59) sharply increases from -43 dB to 0 dB. This is because of the imperfect interpolation induced interference, which agrees well with the trend of the numerical result in [10]. Such high-frequency interference can be alleviated by oversampling the received signal at a relatively high frequency. It is noted that the EVM performance for  $\lambda=1.3$  is close to that for  $\lambda=2.0$ . The best EVM performance on the subcarrier is around -46 dB, which is limited by the DSP precision depending on the designed bit width for a fractional number. Such a low EVM value facilitates application of high level modulation formats of up to 1024-QAM in theory [27,28].



**Fig. 7.** (a) EVM on each subcarrier. (b) EVM comparison between simulation and experiment (ROM).  $Q=4$ , SFO = 100 ppm.

To investigate the impact of SFO on the transmission performance, EVM as a function of SFO is shown in Fig. 7(b). The DSP function blocks at the receiver were simulated with Matlab for comparison. As seen from the figure, the EVM performance with the input signal from the ROM in the experiment is almost identical to the numerical results in the simulation (Matlab). This indicates the validity of the DSP design for the OFDM synchronization. For the perfect sampling case when SFO = 0 and  $\lambda=1$ , the calculated EVM is less than -50 dB. However, for nonzero values of SFO, the EVM performance increases to about -20 dB. This confirms that the EVM performance of the OFDM signal is very sensitive to SFO. As the oversampling rate is increased beyond 1.3, the EVM is improved to around -40 dB.

### 3.2. Real-time VLC transmission performance

After the verification of the synchronization schemes in a single FPGA board, experimental investigation of the real-time OFDM transmission performance was made in the VLC system in Fig. 5. At the AWG-based transmitter, a number of OFDM symbols were generated following the below procedures: 16-QAM mapping, Hermitian symmetry, inverse FFT (IFFT) and insertion of cyclic prefix. For the purpose of the OFDM synchronization, OFDM symbols were arranged according to the frame structure as shown in Fig. 4. The OFDM signal generated offline in Matlab was loaded into the AWG (Tektronix 5014C, 14-bit DAC). The SFO between the transmitter and receiver was induced by varying the sampling rate of the AWG, whilst the sampling rate of the ADC was fixed at 25 MS/s and 50 MS/s for  $\lambda \neq 2$  and  $\lambda=2$ , respectively [10]. Because of discrete values of sampling clocks at the transmitter and receiver, the bit rate of the OFDM signal varies from 25.7 to 43.8 Mb/s. According to the measured transfer function ( $P-U$  curve) of the white



LED in Fig. 5, the bias voltage was 5.75 V, and the peak-to-peak (PTP) voltage of the driving signal was 0.4 V [29]. At the FPGA-based receiver, after optical-to-electrical conversion, the received signal is sampled by an ADC (14-bit) followed by an FPGA board for real-time signal recovery. The transmission distance was 6 m.

Figure 8 shows EVM performance using the 4<sup>th</sup> order interpolator when SFO = 100 ppm. Compared with the EVM performance from the ROM in Fig. 7(a), the EVM on the low frequency subcarriers (1-6) is relatively high due to the baseline wander effect in the low frequency range in the VLC link [24]. These low frequency subcarriers were not used for data transmission or EVM calculation. The minimum EVM is about -23 dB on the 10<sup>th</sup> subcarrier because of the attenuation and noise in the VLC link. The constellations of the received 16-QAM-OFDM signals with SFO = 100 ppm are rotated and dispersed due to the SFO-induced ICI, crosstalk and noise. After SFO compensation using the 4<sup>th</sup> order interpolator ( $\lambda=1.3$ ), the constellation is clear, which proves the effectiveness of the SFO compensation scheme.

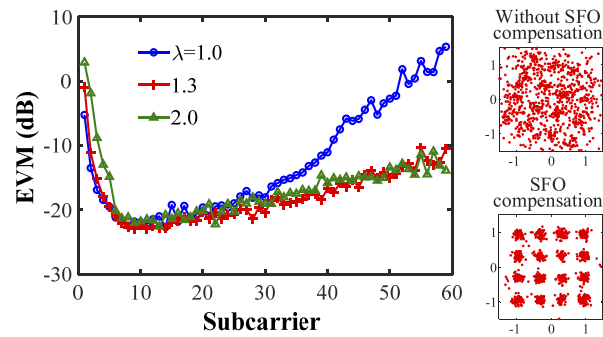
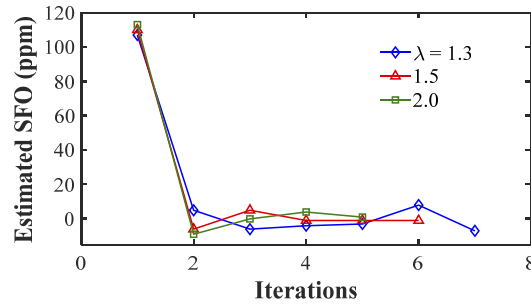


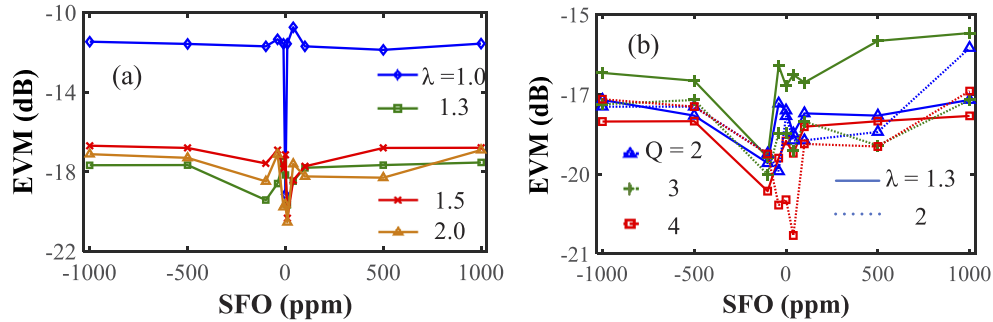
Fig. 8. EVM performance with the 4<sup>th</sup> order interpolator (SFO = 100 ppm).

Estimation of the SFO is important for the signal reconstruction because the sampling frequency of the transmitter/receiver oscillators varies with time or temperature. As an example, in Fig. 9, the estimated SFO curves are plotted when the SFO is set at around 100 ppm. Given that it is difficult to measure an accurate frequency of these oscillators, the specified SFO may not reflect a real SFO value. Therefore, the initial value of the estimated SFO is slightly higher than 100 ppm as seen in Fig. 9. After the initial estimation of SFO, the following OFDM signal is reconstructed so that the SFO estimated with the reconstructed signal is expected to be close to zero. This is confirmed in the figure that the estimated values of SFO after the first SFO estimation converge to zero. However, a small variation in SFO is observed because of the noise in the VLC link. It is noted that the magnitude of the variation in estimated SFO for  $\lambda=1.5$  or 2.0 is smaller than that for  $\lambda=1.3$ . Because of the limited amount of samples stored in the AWG, the number of observed iterations is relatively small for large  $\lambda$ .

Figure 10(a) shows the measured EVM at different oversampling rates with the 4<sup>th</sup> order interpolator. All the EVM values for  $\lambda \geq 1.3$  are below -16.6 dB, which corresponds to a bit error rate (BER) of  $10^{-3}$  for 16-QAM. Compared with the offline results in [10], the EVM degrades by approximately 4 dB because of the imperfect hardware including the ADC. The EVM comparison between the 2<sup>nd</sup>, 3<sup>rd</sup> and 4<sup>th</sup> order polynomial interpolators is shown in Fig. 10(b). The EVM with the 4<sup>th</sup> order interpolator is improved by up to 1 dB compared with the low order interpolator when  $\lambda = 1.3$ . As the oversampling rates increases, the EVM difference between the 2<sup>nd</sup>, 3<sup>rd</sup> and 4<sup>th</sup> order interpolators becomes small. The variation in EVM for large absolute values of SFO may be because of the accumulated phase error in the channel estimation/equalization at a relatively slow update rate of estimated SFO. Such variation can be minimized by applying advanced channel equalization algorithms, which is beyond the scope of this study.



**Fig. 9.** Estimated SFO with the 4<sup>th</sup> interpolator at different oversampling rates ( $\lambda$ ).



**Fig. 10.** (a) Measured EVM versus SFO ( $Q = 4$ ), (b) EVM performance with the 2<sup>nd</sup>, 3<sup>rd</sup> and 4<sup>th</sup> order interpolators.

Table 2 shows the DSP complexity of different interpolators in the report of the hardware compilation for the DSP design. The consumed resources of hardware and latency increase with the order of the digital interpolator. Compared with the 2<sup>nd</sup> order interpolator, the consumed resources for the 3<sup>rd</sup> order interpolator are increased by at least 50%, whilst the 4<sup>th</sup> order interpolator almost doubles the latency. In general, the DSP complexity for the 4<sup>th</sup> order interpolator increases by a factor of 2 to 7. The consumed DSP48E, slice registers and logic resources (slice LUTs, occupied slices and LUT flip-flop pairs) are about 2, 3, and 4 times that for the 3<sup>rd</sup> order interpolator, respectively. As a result, a high order digital interpolator can be used to effectively compensate SFO at the cost of DSP complexity, which however results in a reduced oversampling rate of ADC. This can relax the requirement for ADCs in terms of sampling speed and stability of the oscillators. Moreover, the consumed resources takes a small amount of the whole available sources on the FPGA board. Therefore, high order digital interpolators are still

**Table 2. Comparison in DSP complexity of the Farrow-structured interpolators**

Resource	Available	$Q = 2$	$Q = 3$	$Q = 4$
Slice LUTs	80,000	611	1020	4388
Slice registers	160,000	631	932	2798
Occupied slices	20,000	190	336	1479
LUT flip-flop pairs	18,300	694	1159	4591
DSP48E	480	5	9	18
Latency (sample period)	-	9	12	17

promising solution for future VLC applications as modern digital electronics grows fast in recent years.

#### 4. Conclusion

A real-time OFDM-VLC receiver incorporating the designed digital interpolation-based SFO compensation has been successfully demonstrated with commercially available LEDs and DACs/ADCs. It has shown that based on a designed OFDM frame structure the real-time OFDM transmission performance with the 2<sup>nd</sup>/3<sup>rd</sup>/4<sup>th</sup> order Farrow-structured interpolator is robust to SFO up to  $\pm 1000$  ppm. A trade-off between the DSP complexity and oversampling rate at the receiver has been recognized. Compared with the low order interpolators, the EVM with the 4<sup>th</sup> order interpolator is improved by up to 1 dB, whilst the DSP complexity increases by a factor of 2 to 7. Moreover, the consumed hardware resources take a small amount of the whole available sources on the FPGA board, which makes the high order digital interpolator-based SFO compensation promising for future short-range VLC applications. In addition, it has been observed that the latency of DSP results in a relatively slow update rate of estimated SFO, which may affect the EVM performance for large SFO. The optimization of the DSP latency related to estimation of SFO and CSI will be studied in the future.

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#### Disclosures

The authors declare no conflicts of interest.

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